



**Samueli**  
Computer Science



CIKM Applied Research Paper

# **P-Companion: A Principled Framework for Diversified Complementary Product Recommendation**

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## ➔ Background: Complementary Product Recommendation (CPR)

- Behavior-based Product Graphs (BPG)
- P-Companion Model
- Experiments & Case Study
- Summary & Future work

# What to buy together?

## Frequently bought together



Total price: **\$149.67**

Add all three to Cart

Add all three to List

One of these items ships sooner than the other. [Show details](#)

- ✓ **This item:** HP OfficeJet 3830 All-in-One Wireless Printer, HP Instant Ink, Works with Alexa (K7V40A) **\$99.89**
- ✓ **HP 63 | Ink Cartridge | Black | F6U62AN** **\$20.89**
- ✓ **HP 63 | Ink Cartridge | Tri-color | F6U61AN** **\$28.89**

## Customers who bought this item also bought



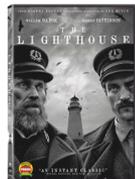
Prometo  
Pablo Alborán  
★★★★☆ 187  
Audio CD  
**\$16.41**



Pablo Alborán  
Pablo Alborán  
★★★★☆ 135  
Audio CD  
**\$9.28**



Hotspot  
PET SHOP BOYS  
★★★★☆ 449  
Audio CD  
**\$11.19**  
prime FREE One-Day



Lighthouse, The  
Robert Pattinson  
★★★★☆ 3,985  
DVD  
**\$12.99**  
prime FREE One-Day

Added to Cart  
Cart Subtotal (1 Item): \$99.70  
View Cart Proceed to checkout

### Customers who bought this item also bought

- Quality Premium Adult Removable Duvet Cover for Weighted Blanket | 60"x80" | Full Size Bed | 100% Cotton Cover Fabric | Blue  
★★★★☆ 218  
**\$31.92** prime  
Add to Cart
- Quality Premium Adult Removable Duvet Cover for Weighted Blanket | 60"x80" | Full Size Bed | 100% Cotton Cover Fabric | Grey  
★★★★☆ 218  
**\$31.92** prime  
Add to Cart
- Amazon.com Gift Card in a Greeting Card (Various Designs)  
★★★★☆ 13,406  
**\$10.00 - \$2,000.00**  
Choose options

See More

# Complementary Recommendation

Think about one customer who plans to buy a tennis racket (e.g., Head SpeedX Djokovic racket).

What would you recommend for him to purchase together?

- List 1: three more tennis rackets? → **Sorry, we are not looking for substitutes!**
- List 2: three sets of tennis balls? → **Hmm, not bad, but only need one is good enough. Can we do better?**
- List 3: one tennis ball pack, one bag and one headband? → **Sound good this time!**



# Problem Definition

Given the input as catalog features (including item type) and customers behavior data, for a query item  $i$ , we recommend a set of items  $S(i)$ , aiming at optimizing their co-purchase probability and recommendation diversity.



Query item  $i$



Related and diverse recommendation set  $S(i)$

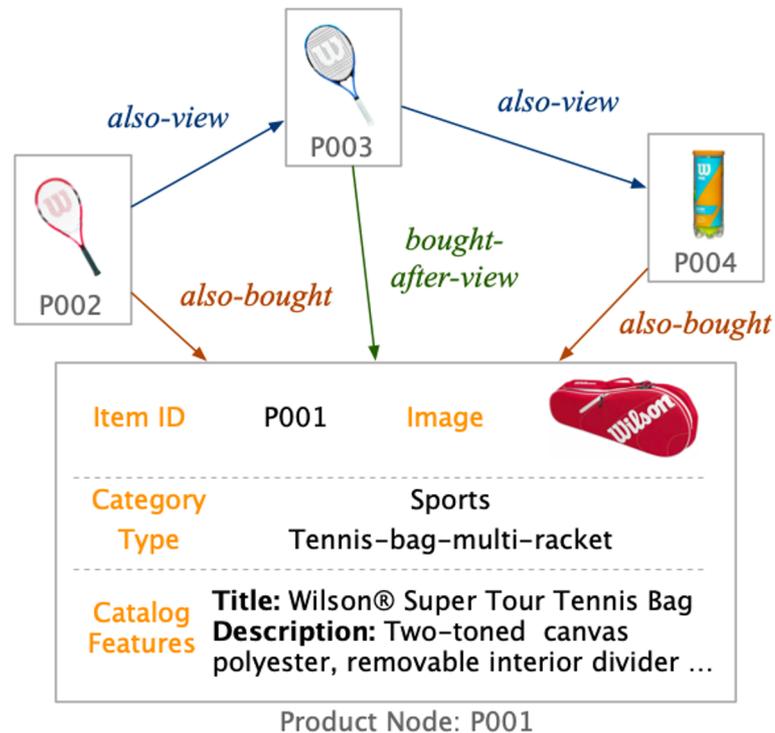
- Background: Complementary Product Recommendation (CPR)

## Behavior-based Product Graphs (BPG)

- P-Companion Model
- Experiments & Case Study
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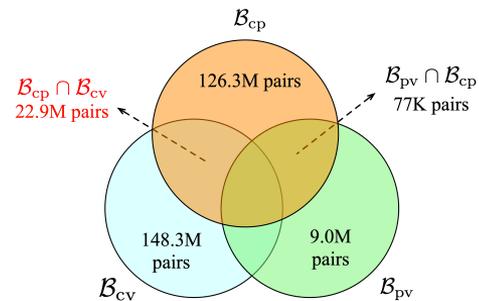
# Behavior-based Product Graphs

- Build a behavior-based product graph
- **Nodes:** Product items with attributes (title, description, category, keywords)
- **Edges:** Customer browsing and purchase behaviors (such as **also-bought**, **also-view**, **bought-after-view**, as important indicators of **substitutes** or **complements**)



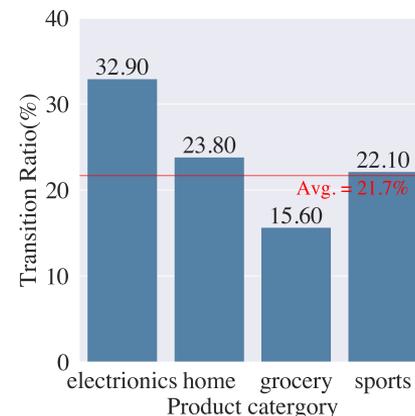
## Two important observations:

1. Product pairs from co-purchase and co-view records are not disjoint, and the amount of overlap heavily depends on categories.
2. Complementary relation in products is often observed across multiple categories.



## Solution: Distant Supervision Collection for Complementary Recommendation

1. We use a subset of co-purchase, i.e.  $\mathcal{B}_{cp} - (\mathcal{B}_{pv} \cup \mathcal{B}_{cv})$  as labels for complementary products, which contains product pairs only in co-purchase records gives us the complement signals.
2. Removed the restriction of making recommendations within one category in and create a general dataset with multiple categories.

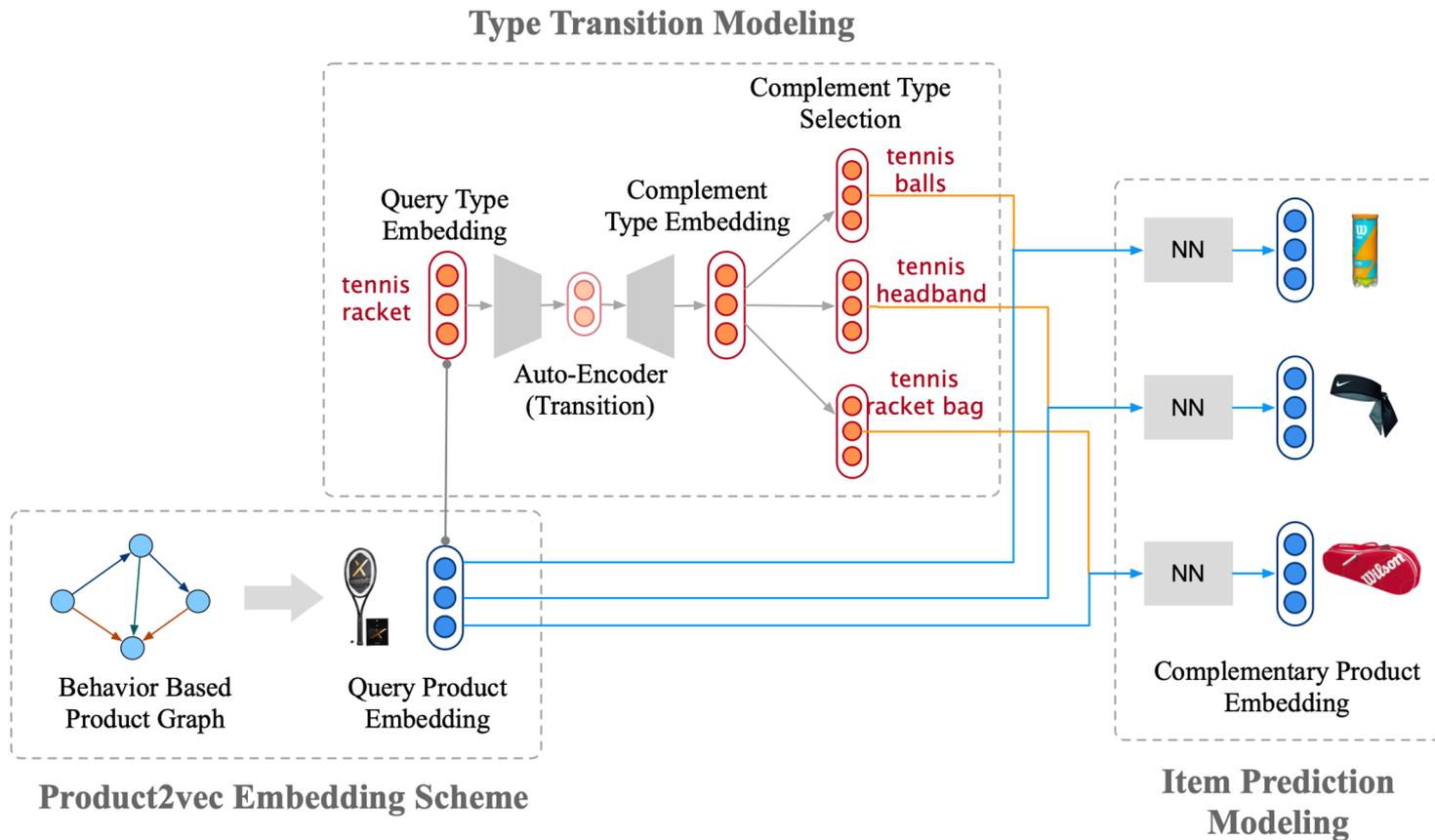


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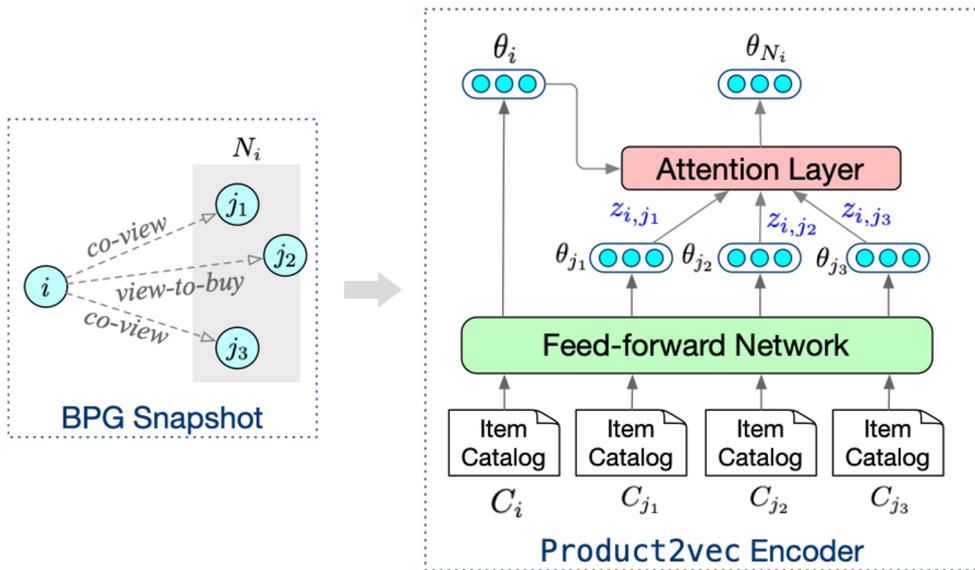
## P-Companion Model

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# P-Companion: Overview



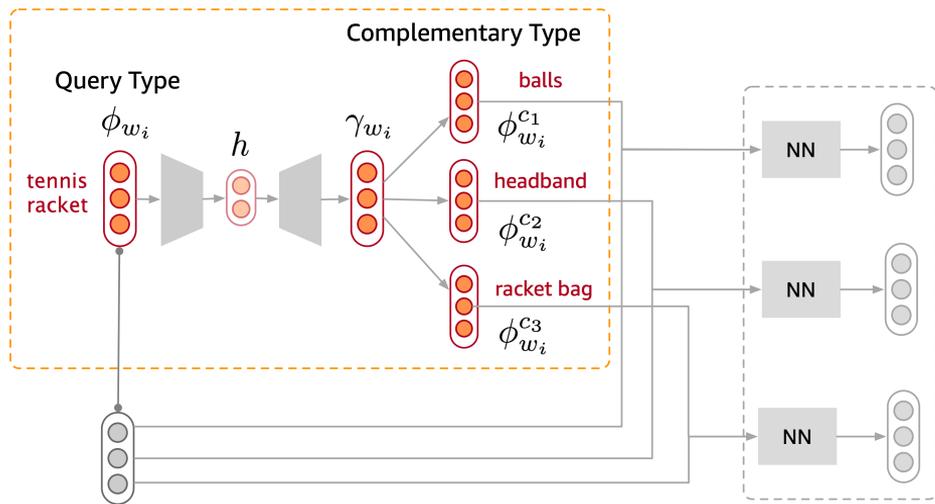
- GNN-based representation learning framework for millions of products.
- FNN transforms the original item catalog features to embeddings and later aggregates the information from similar products selectively by the attention layer.
- After training, FNN can be applied to obtain product embeddings for millions of products, including cold-start ones, which are used for subsequent modules.



# Module 2: Complementary Type Transition

**Goal:** (1) Model the asymmetric relationship between query product type and complementary product types; (2) Generate diversified complementary product types for further item recommendation.

## Type Transition Modeling



Auto-encoder based type transition model:

$$h = \text{Dropout} \left( \text{ReLU} \left( \phi_{w_i} W^{(4)} + b^{(4)} \right) \right)$$

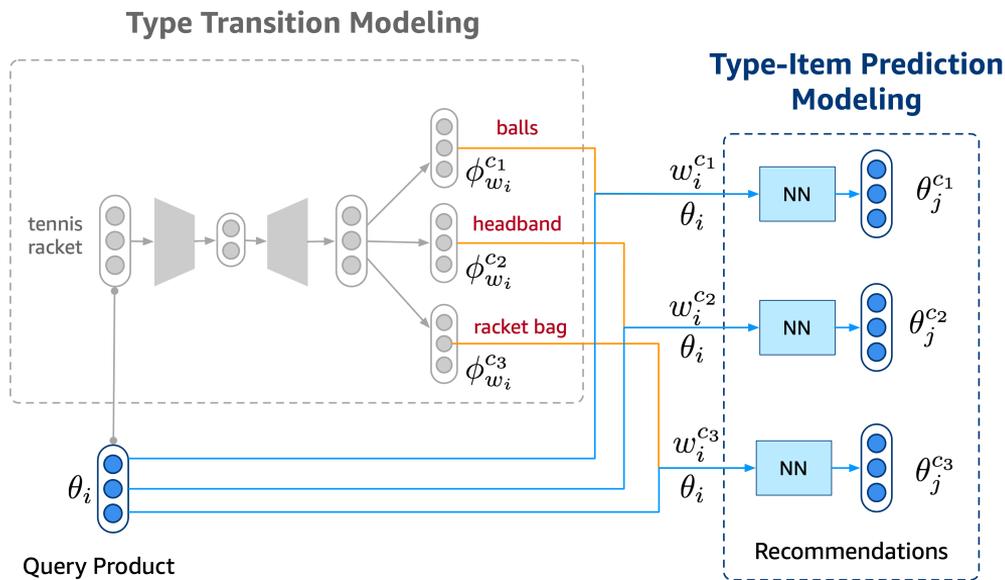
$$\gamma_{w_i} = h W^{(5)} + b^{(5)}$$

Training loss:

$$\min \sum_{i,j \in \mathcal{T}} \left( \max \left\{ 0, \epsilon_w - y_{i,j} \left( \lambda_w - \|\gamma_{w_i} - \phi_{w_j}^c\|_2^2 \right) \right\} \right)$$

# Module 3: Complementary Item Prediction

**Goal:** Output item recommendations given the embeddings of query product and inferred multiple complementary types.



Item prediction neural model:

$$\theta_i^{w_c} = \theta_i \odot (\phi_{w_c}^c W^{(6)} + b^{(6)}),$$
$$s.t., \|\phi_{w_c}^c - \gamma_{w_i}\|_2^2 \leq \beta$$

Training loss:

$$\min \sum_{i,j \in \mathcal{T}} \max \{0, \epsilon_i - y_{i,j} (\lambda_i - \|\theta_i^{w_c} - \theta_j\|_2^2)\}$$

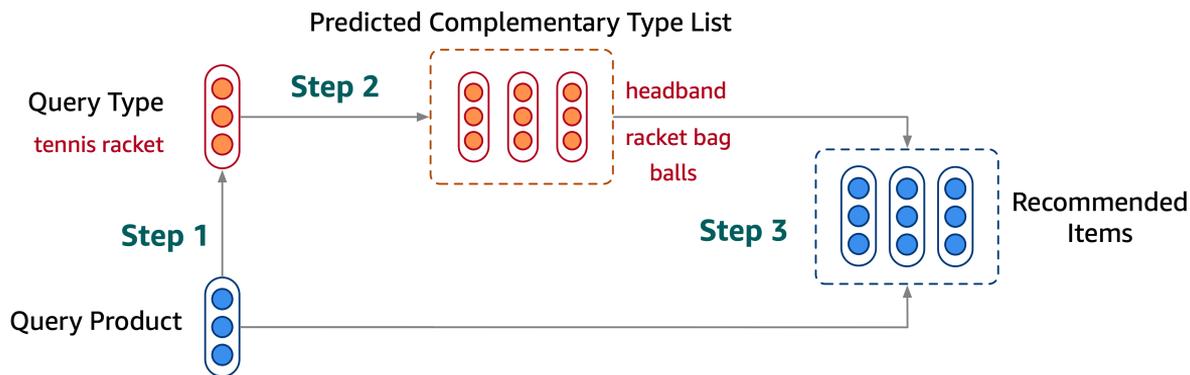
Joint training on type transition and item prediction:

$$\min \sum_{i,j \in \mathcal{T}} \alpha \left( \max \left\{ 0, \epsilon_i - y_{i,j} \left( \lambda_i - \|\theta_i^{w_j} - \theta_j\|_2^2 \right) \right\} \right) + (1 - \alpha) \left( \max \left\{ 0, \epsilon_w - y_{i,j} \left( \lambda_w - \|\gamma_{w_i} - \phi_{w_j}^c\|_2^2 \right) \right\} \right)$$

Item prediction loss

Type transition loss

Inference stage:



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# Evaluation: Dataset

- We evaluate P-Companion a real-world dataset obtained from Amazon.com, which includes over 24M of products with catalog features and customer behavioral data across 10+ product categories.
- For comparison with baselines, we also select grocery and electronics category as two subsets from Amazon.

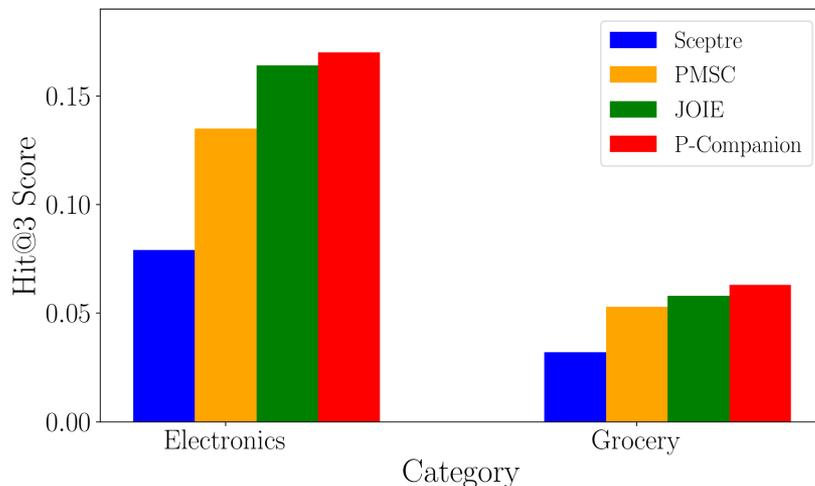
amazon



Datasets	Electronics	Grocery	All Groups
# Items	97.6K	324.2K	24.54M
# Product Types	5.6K	6.5K	34.8K
# Co-purchase pairs	130.6K	804.1K	62.16M
# Co-view pairs	3.15M	8.96M	1154M
# purchase-after-view pairs	325.1K	1.10M	83.75M

# Evaluation: From history purchase data

- Given a pair  $(i, j)$ , associated with type  $w_i$  and  $w_j$ , from co-purchase record as ground truth, we ask our model as well as all baselines to output recommendation list (with predicted complementary types), and consider the following:
  - whether item  $j$  is in the list.  $\rightarrow$  *Item level*
  - Whether type  $w_j$  is in the predicted types  $\rightarrow$  *Type level*
- Metric: Hit@K score, Baselines: Sceptre, PMSC, JOIE



Dataset		Electronics	Grocery
Model & Setting		Hit@60	Hit@60
Sceptre		0.124	0.085
PMSC		0.179	0.139
JOIE		0.200	0.155
P-Companion	1 type $\times$ 60 items	0.138	0.088
	3 types $\times$ 20 items	0.198	0.153
	5 types $\times$ 12 items	0.222	<b>0.189</b>
	6 types $\times$ 10 items	<b>0.227</b>	0.187

# Case Study: Type Transition Prediction

## Examples of Predicted Top-3 Complementary Type Predictions

Query Type	Predicted Complementary Types
camera-power-adapter	(1) sec-digit-card (2) micro-sd-card (3) hdmi-cable
cell-phone-battery	(1) cell-phone-screen-protect (2) battery-charge-case (3) flip-cell-phone-carry-case
roast-coffee-bean	(1) fridge-coffee-cream (2) whole-bean (3) white-tea
fly-fish-line	(1) fluorocarbon-fish-line (2) surf-fish-rod (3) fly-fish-reel

# Case Study: Product Recommendation

Category	Query Item	Co-Purchase	Top-5 Recommendations from P-Companion
Electronics			    
Grocery			     
All-Group (Pet home)		None	    
All-Group (Fishing tools)		None	    

# Evaluation: Online Deployment

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- After deploying P-Companion for online serving, we conduct online A/B testing on Amazon by splitting customer sessions randomly.
- For the control group, we use co-purchase datasets for the recommendation, while for the treatment group, we show recommendations from P-Companion.
- We observe relative **+0.23%** improvement on product sales, **+0.18%** improvement on profit gain, by considering both diversity and relevance in P-Companion.

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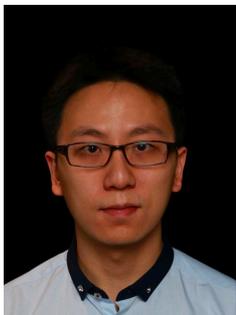
# Summary & Future Directions

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- **Model:** P-Companion, an end-to-end neural-based recommendation solution for diversified complementary product recommendation.
- **Data:** a novel schema to obtain improved distant supervision labels for better complementary model learning on multiple categories of products.
- **Performance:** Experimental evaluation has shown the effectiveness in recommending relevant and diversified complementary items over alternative approaches and demonstrated strong business values on our online production systems.
- **Future directions of P-Companion:** (1) adaptive diversified recommendation for different categories; (2) leveraging temporal customer purchase history information to generate personalized complementary recommendations.

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# Thank you!

Q & A